

# "Do-and-don't" for S2 statistics

*S2 binomial, Poisson, normal, uniform*

**DO: # Know discrete is |||||  
and continuous is \_\_\_\_\_**

**# Know binomial is discrete  
and like number of heads when  
tossing coins**

**# Know Poisson is discrete and  
like number of goals when  
playing football**

**# Know normal is continuous  
and like errors in a  
manufacturing process**

**# Know the continuous  
uniform distribution is  
continuous and like waiting time for a train which goes  
exactly every 20 minutes**

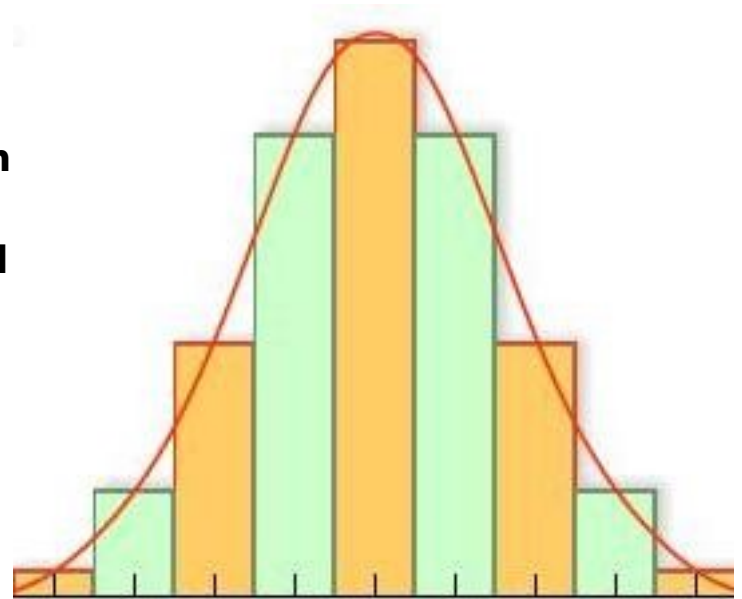
**# Know binomial  $\rightarrow$  Poisson as  $n$  becomes large with  $p$  fixed  
and small ( $<0.05$ )**

**# Know binomial  $\rightarrow$  normal as  $n$  becomes large (for any  $p$ , but  
especially middling  $p$ )**

**# Know Poisson  $\rightarrow$  normal as  $\lambda$  becomes large**

**# When using normal approx to binomial and Poisson, do  
continuity correction:  $P(\text{binom or Poisson variable is some  
whole number values}) \cong P(\text{normal variable is any number  
which rounds to those whole number values})$**

**# Learn by heart the conditions for when to use distributions  
<http://www.memrise.com/course/336931/a-level-maths-edexcel-s2/>**



**DON'T # Fail to make continuity correction**

**DO # Think:  $P(\text{binom or Poisson variable is some whole number values}) \cong P(\text{normal variable is any number which rounds to those whole number values})$**

**DON'T # Look up or calculate  $P(X=n)$  when you want  $P(X \leq n)$ , or vice versa**

**DO # Always write out the  $P$  you're looking up or calculating,  $P(X \leq n)$ ; or  $P(X=n)$ ; or  $P(X > n)$ , which is  $1 - P(X \leq n)$ ; etc.**

**DON'T # Write e.g.  $X \sim B(100, 0.05)$  without saying what  $X$  is**

**DO # When you use approximations, be clear, e.g.:**

**$X \sim B(100, 0.05) \approx \text{Po}(5)$  or  $X \sim B(100, 0.2) \approx N(50, 40)$  or  $X \sim \text{Po}(50) \approx N(50, 50)$**

## S2 hypothesis testing and sampling

**DO: # State  $H_0$  = *null hypothesis* = default belief in absence of new evidence, e.g. coin is unbiased, medicine makes no difference**

**DO: # State  $H_1$  = *alternative hypothesis* = suggestion to be checked, e.g. coin is biased, medicine helps cure you**

**DO: # State  $H_1$  as *one-tailed*, e.g. test whether coin biased to heads alone, or *two-tailed*, e.g. coin biased either way**

**DO: # State *significance level* = your standard of how improbable a result has to be on the assumption of  $H_0$  for you to reject  $H_0$  and go for  $H_1$**

**DO: # State *critical region* = range of results (one-tailed or two-tailed) which is so far out from what's expected with  $H_0$  that probability < significance level**

**DO: # State *actual significance level* = probability of result being in critical region (i.e. less than pre-set significance level)**

**DO: # *Draw a picture* of the range of possible results and the critical region, double-checking on one tail or two**

DO # Learn definitions about sampling by heart:

<http://www.memrise.com/course/336931/a-level-maths-edexcel-s2/>.

DON'T # Mix up  $H_0$  and  $H_1$ .

DO # Remember  $H_0$  is what you would go for with 0 (zero) new evidence

DON'T # Get continuity corrections wrong if you're using Normal approximation

DO # Think:  $P(\text{binom or Poisson variable is some whole number values}) = P(\text{normal variable is any number which rounds to those whole number values})$

DON'T # Think or write that a result *proves*  $H_0$  (or  $H_1$ ). Think, and write: "The evidence is not enough to reject  $H_0$ " or "The evidence is enough to reject  $H_0$ ". And write what it means: "The evidence is enough to suggest the coin is biased", or "the evidence is not enough to suggest the coin is biased".

**DO: # calculate  $E(X) = \sum x_i p(x_i)$  or  $= \int x f(x) dx$**

**DO: # calculate  $E(X^2) = \sum x_i^2 p(x_i)$  or  $= \int x^2 f(x) dx$**

**DO: # calculate  $\text{var}(x) = (E(X^2)) - (E(X))^2$**

**DO: # Remember probability density function  $f(x)$  does not measure a probability. For a continuous random variable,  $p(\text{any given value}) = 0$ . Any function  $f(x)$  can be a pdf if  $f(x) \geq 0$  for all  $x$  and  $\int_{-\infty}^{\infty} f(x) dx = 1$**

**DO: # Calculate cumulative distribution function**

**$F(x) = \int_{-\infty}^x f(t) dt$  is a probability.  $F$  must be continuous, always increasing, and  $\rightarrow 1$  as  $x \rightarrow \infty$**

**DO # Calculate median by  $F(m) = 0.5$**

**DO # Calculate skew as the opposite of what you'd think: if the graph is tilted to the right, that's negative skew**

**DON'T # Fail to show values of  $F$  for the whole range (usually  $F$  is 0 for a whole range of low  $x$ , and 1 for a whole range of high  $x$ )**

**DON'T # Fail to "fit together" the values of  $F$  at the points where different functions defining it join.**

**DO # When you introduce each random variable  $X$ , say what it is, e.g.  $X = \text{number of heads from 20 tosses of coin}$ .**

**DO # Use capitals for random variables.**